



# REST AND MOTION



## DISTANCE

- The length of the actual path traversed by the particle is termed as its distance.
- Distance =  $S$  = length of path ACB.
- Scalar quantity and is measured in meter. It can never decrease with time.



## DISPLACEMENT

- The change in position vector of the particle for a given time interval is known as its displacement.
- Displacement =  $B - A$
- It can decrease with time. Vector quantity and is measured in meter.

## AVERAGE VELOCITY

$$\text{Average Velocity } (\bar{v}_{av}) = \frac{\text{Total Displacement}}{\text{Total Time Taken}} = \frac{\vec{B} - \vec{A}}{t}$$

## AVERAGE SPEED

$$\text{Average Speed } (v_{av}) = \frac{\text{Total Distance Travelled}}{\text{Total Time Taken}} = \frac{S}{t}$$

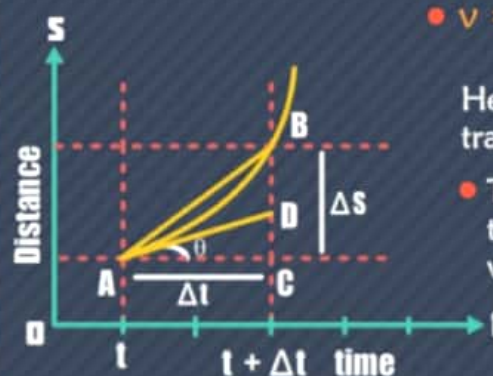
## INSTANTANEOUS SPEED

- The instantaneous speed is the speed at a particular instant of time.

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt}$$

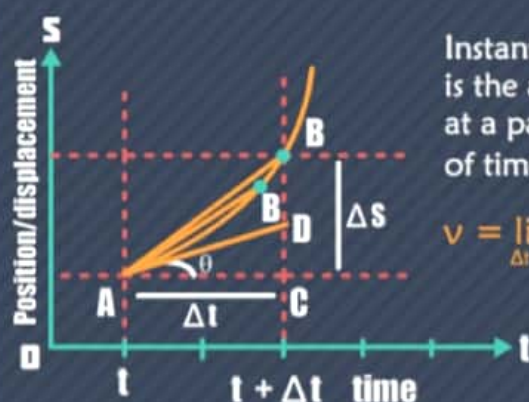
Here  $\Delta s$  is the distance travelled in time  $\Delta t$ .

- The slope of the tangent equal  $ds/dt$ , which is equal to the instantaneous speed at 't'.



$$v = \tan(\theta) = \frac{DC}{AC} = \frac{ds}{dt}$$

## INSTANTANEOUS VELOCITY



Instantaneous velocity is the average velocity at a particular instant of time.

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta r}{\Delta t} = \frac{dr}{dt}$$

## EQUATIONS OF MOTION

1.  $v = u + at$
2.  $v^2 - u^2 = 2as$
3.  $s = ut + \frac{1}{2}at^2$
4.  $s_{nth} = u + \frac{a}{2}(2n - 1)$

## REACTION TIME



It's the difference between the time when one see a situation to the time when one acts.

$$\text{Reaction Time } \Delta t = t_2 - t_1$$

## ACCELERATION

When the velocity of a moving object/particle changes with time, we can say that it is accelerated.

### Average Acceleration

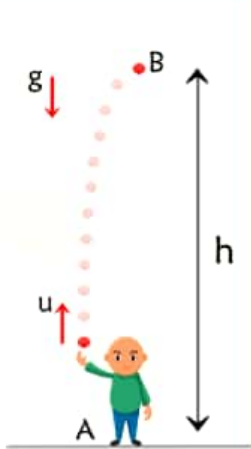
$$a_{av} = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1} = \frac{\Delta \vec{v}}{\Delta t}$$

### Instantaneous Acceleration

$$\vec{a} = \lim_{\Delta t \rightarrow 0} \vec{a}_{av} = \frac{d\vec{v}}{dt}$$



# MOTION UNDER GRAVITY

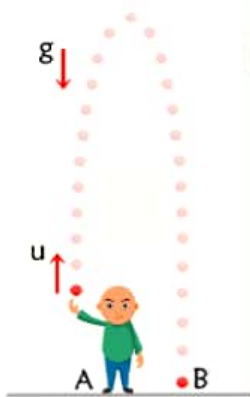


## Sign Conventions

$$\begin{aligned} u &= +ve \\ h &= +ve \\ v &= 0 \\ a &= -g \end{aligned}$$

## Equation of motion

$$\begin{aligned} h &= ut - \frac{1}{2}gt^2 \\ 0 &= u - gt \\ 0^2 &= u^2 - 2gh \end{aligned}$$

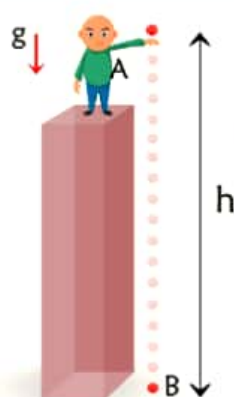


## Sign Conventions

$$\begin{aligned} u &= +ve \\ h &= 0 \\ v &= -ve \\ a &= -g \end{aligned}$$

## Equation of motion

$$\begin{aligned} 0 &= ut - \frac{1}{2}gt^2 \\ -v &= u - gt \\ v^2 &= u^2 - 2g(0) \end{aligned}$$

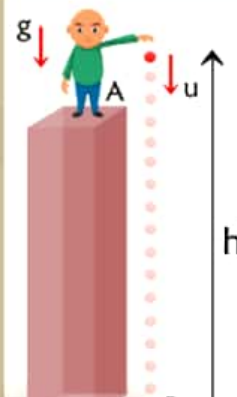


## Sign Conventions

$$\begin{aligned} u &= 0 \\ h &= -ve \\ v &= -ve \\ a &= -g \end{aligned}$$

## Equation of motion

$$\begin{aligned} -h &= 0(t) - \frac{1}{2}gt^2 \\ -v &= 0 - gt \\ v^2 &= (0)^2 + 2gh \\ v &= \pm\sqrt{2gh} \end{aligned}$$

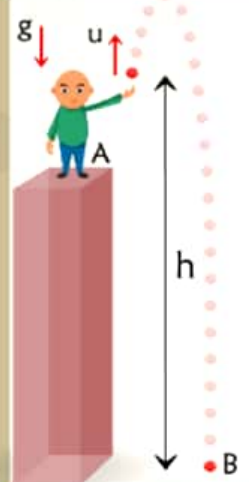


## Sign Conventions

$$\begin{aligned} u &= -ve \\ v &= -ve \\ a &= -g \\ h &= -ve \end{aligned}$$

## Equation of motion

$$\begin{aligned} -h &= -ut - \frac{1}{2}gt^2 \\ -v &= -u - gt \\ v^2 &= u^2 + 2gh \end{aligned}$$



## Sign Conventions

$$\begin{aligned} u &= +ve \\ v &= -ve \\ a &= -g \\ h &= -ve \end{aligned}$$

## Equation of motion

$$\begin{aligned} -h &= ut - \frac{1}{2}gt^2 \\ -v &= u - gt \\ v^2 &= u^2 + 2gh \end{aligned}$$



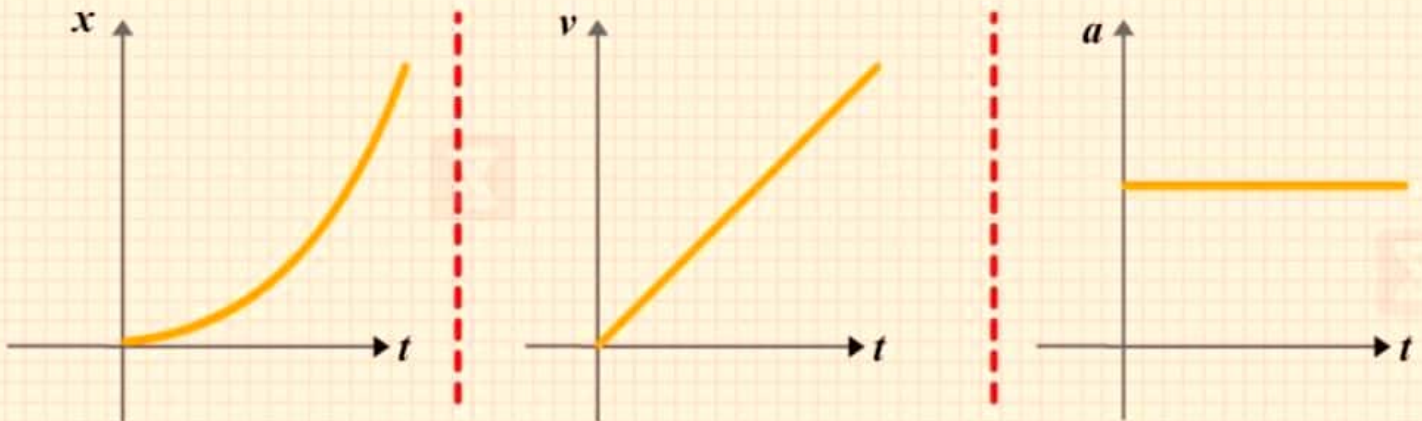
# RECTILINEAR MOTION CASES

Distance

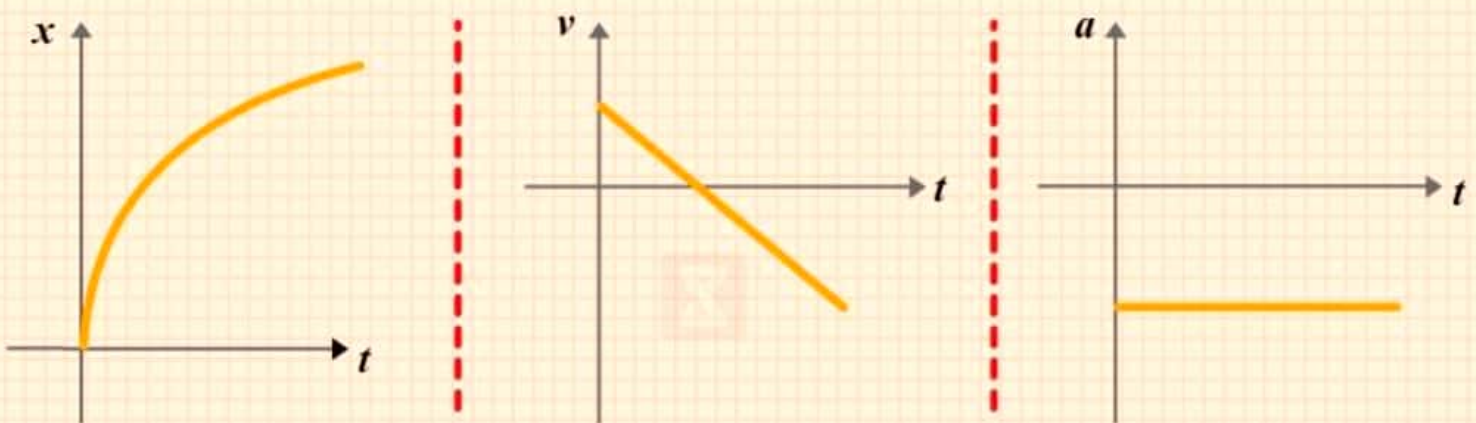
Velocity

Acceleration

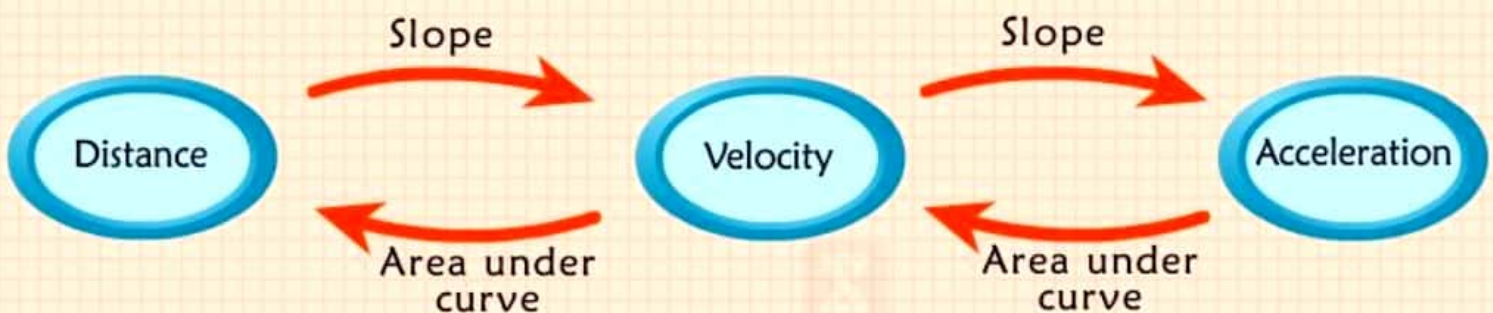
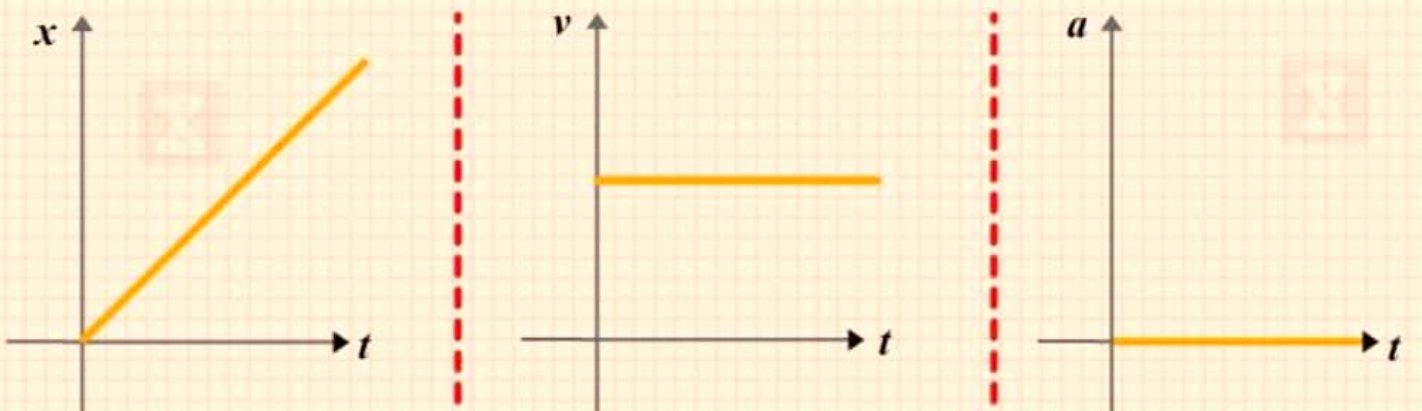
BODY MOVING WITH INCREASING VELOCITY



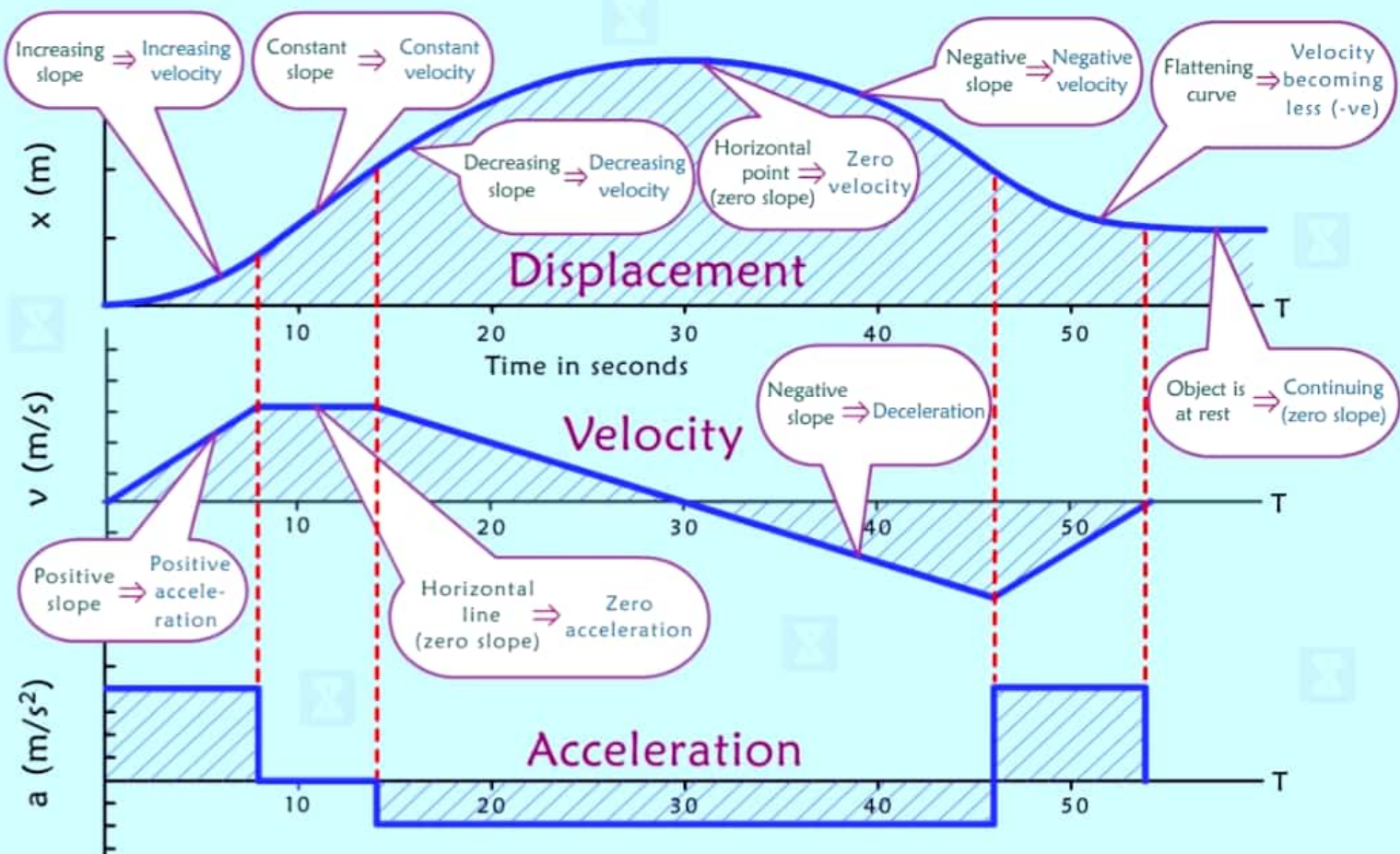
BODY MOVING WITH DECREASING VELOCITY



BODY MOVING WITH UNIFORM VELOCITY



## DISPLACEMENT, VELOCITY AND ACCELERATION GRAPH





# RELATIVE VELOCITY



Relative velocity of A wrt B

$$\vec{V}_{AB} = \vec{V}_A - \vec{V}_B$$

Relative acceleration of A wrt B

$$\vec{a}_{AB} = \vec{a}_A - \vec{a}_B$$



## RIVER-BOAT PROBLEM

$\vec{V}_r$  = absolute velocity of river

$\vec{V}_{br}$  = velocity of boatman with respect to river or velocity of boatman in still water

$\vec{V}_b$  = absolute velocity of boatman.



Time taken by boatman to cross the river:

$$t = \frac{W}{V_{br} \cos \theta}$$

Displacement along x-axis when he reaches on the other bank:

$$x = (V_r - V_{br} \sin \theta) \frac{W}{V_{br} \cos \theta}$$



$$\vec{V}_b = \vec{V}_{br} + \vec{V}_r$$

1. Condition when the boatman crosses the river in shortest interval of time-

$$t_{min} = \frac{W}{V_{br}}$$

2. Condition when the boatman wants to reach point B, i.e., at a point just opposite from where he started

$$\theta = \sin^{-1} \left( \frac{V_r}{V_{br}} \right)$$

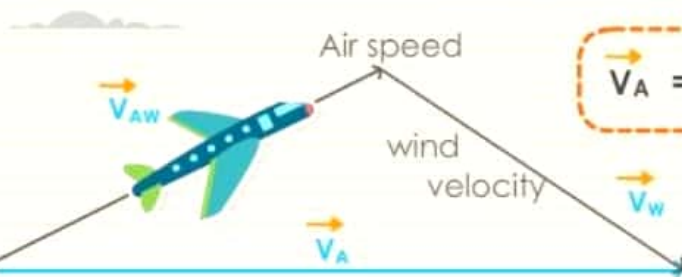
3. Shortest Path

when  $V_r < V_{br} \rightarrow S_{min} = W$

when  $V_r > V_{br} \rightarrow$

$$S_{min} = W \left( \frac{V_r}{V_{br}} \right)$$

## AIRCRAFT WIND PROBLEM



$$\vec{V}_A = \vec{V}_{AW} + \vec{V}_W$$

$\vec{V}_{AW}$  = Velocity of aircraft wrt wind

$\vec{V}_W$  = Velocity of wind

$\vec{V}_A$  = Absolute Velocity of aircraft

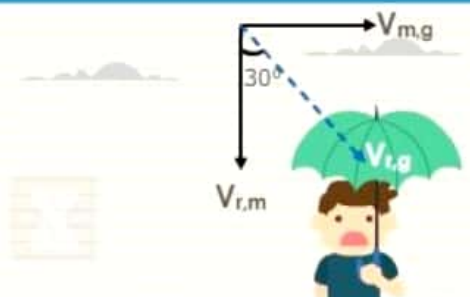
## RAIN PROBLEM

$\vec{V}_{r,g}$  = Velocity of river wrt ground

$\vec{V}_{r,m}$  = Velocity of river wrt man

$\vec{V}_{m,g}$  = Velocity of man wrt ground

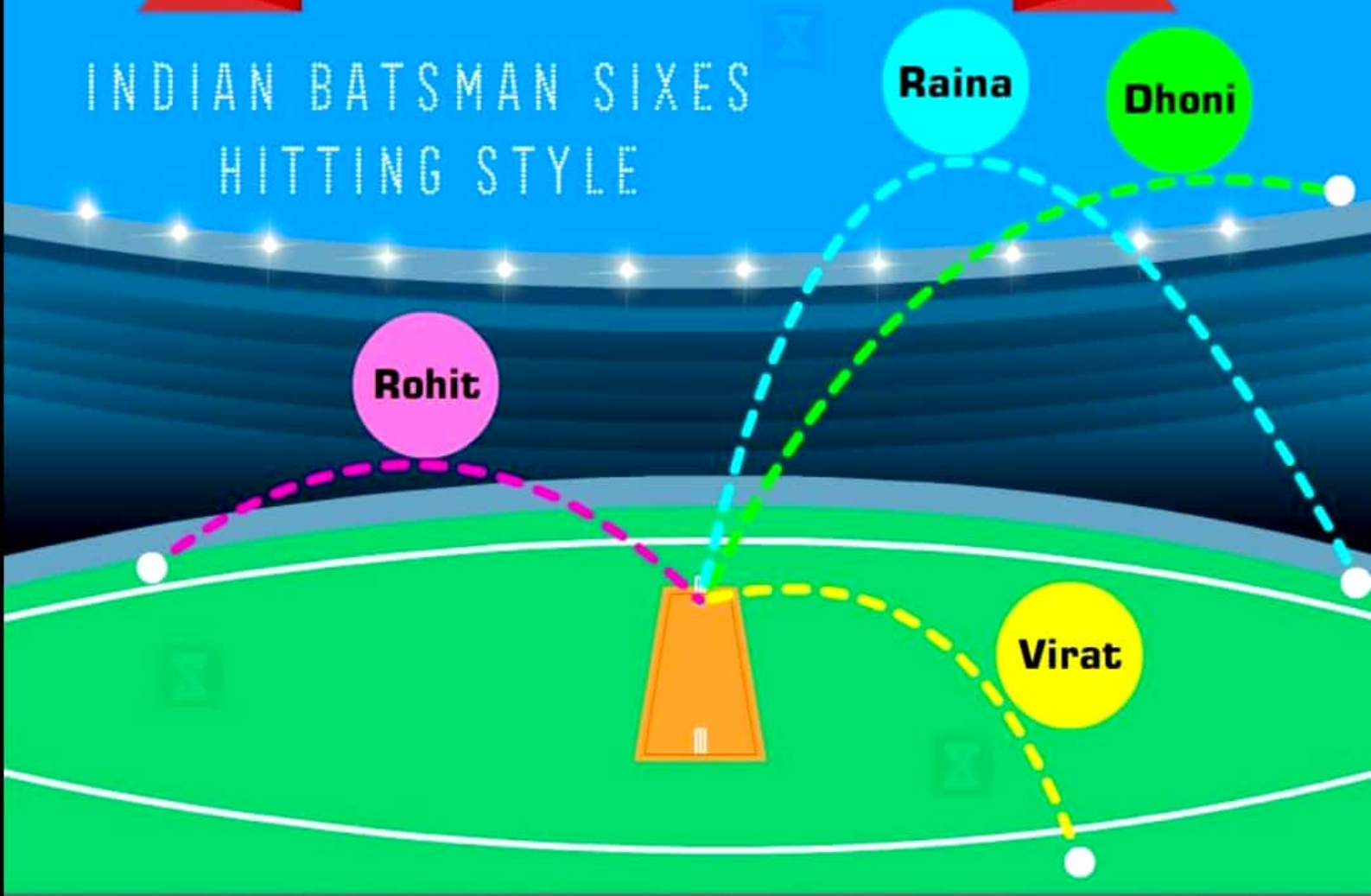
$$\vec{V}_{r,g} = \vec{V}_{r,m} + \vec{V}_{m,g}$$



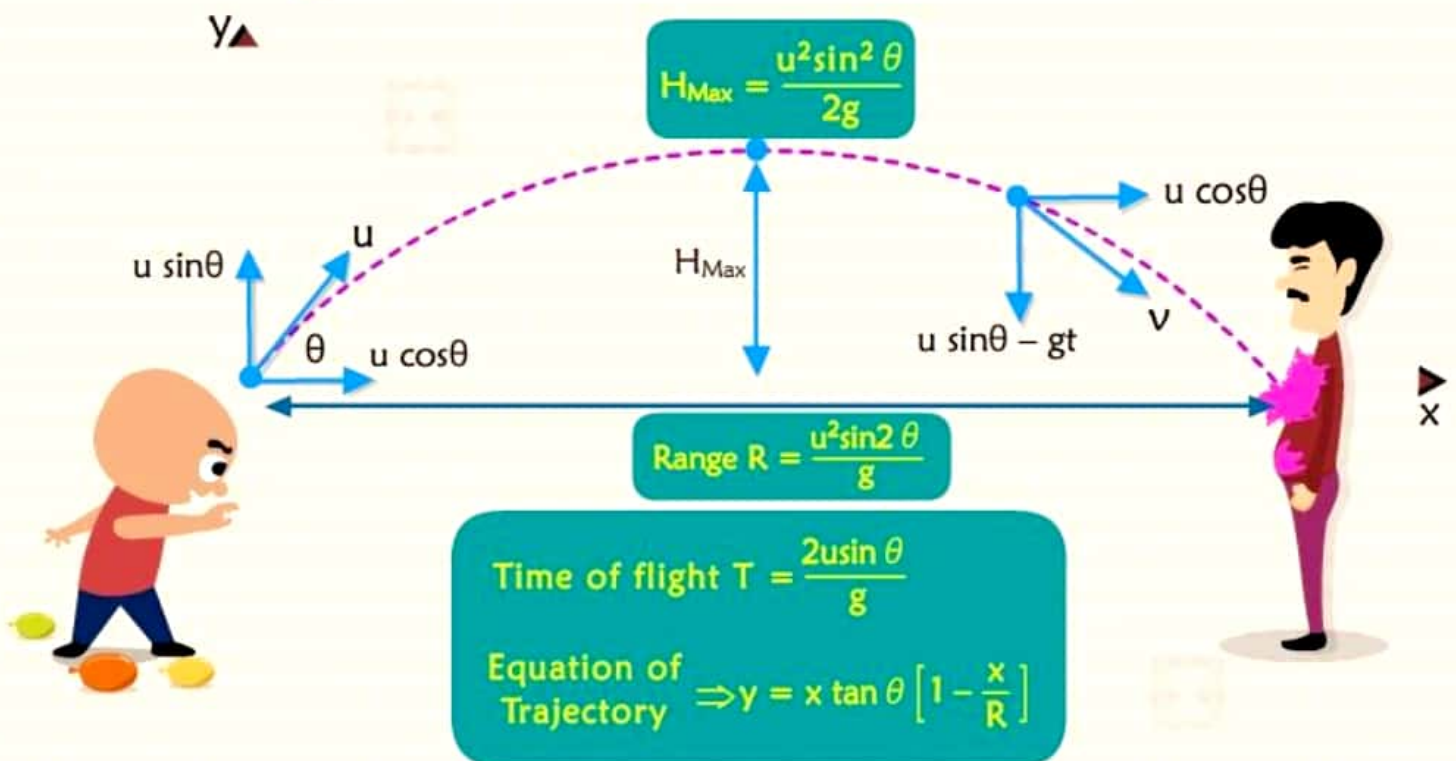
# PROJECTILE MOTION

Part I

INDIAN BATSMAN SIXES  
HITTING STYLE

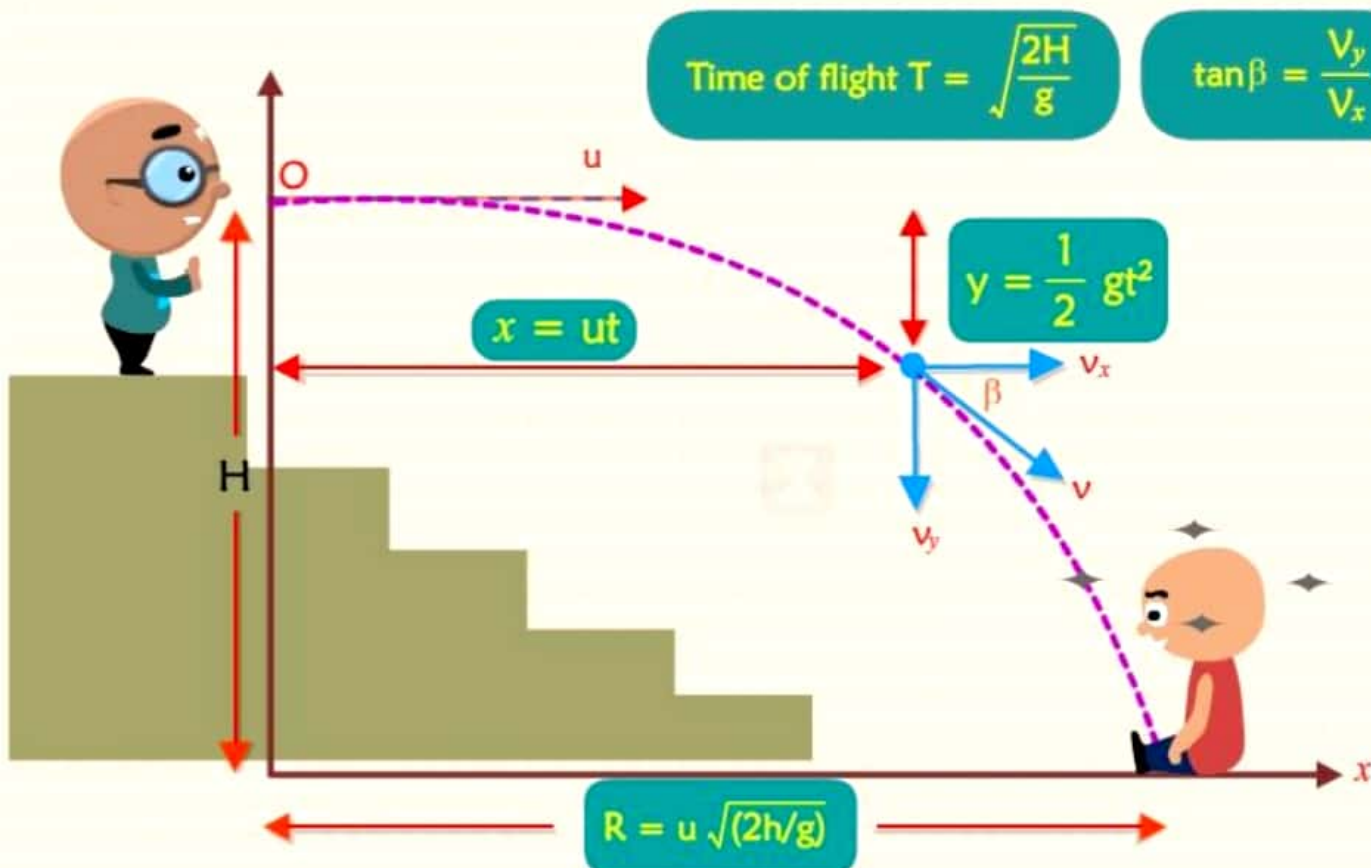


## 1 BASIC PROJECTILE MOTION

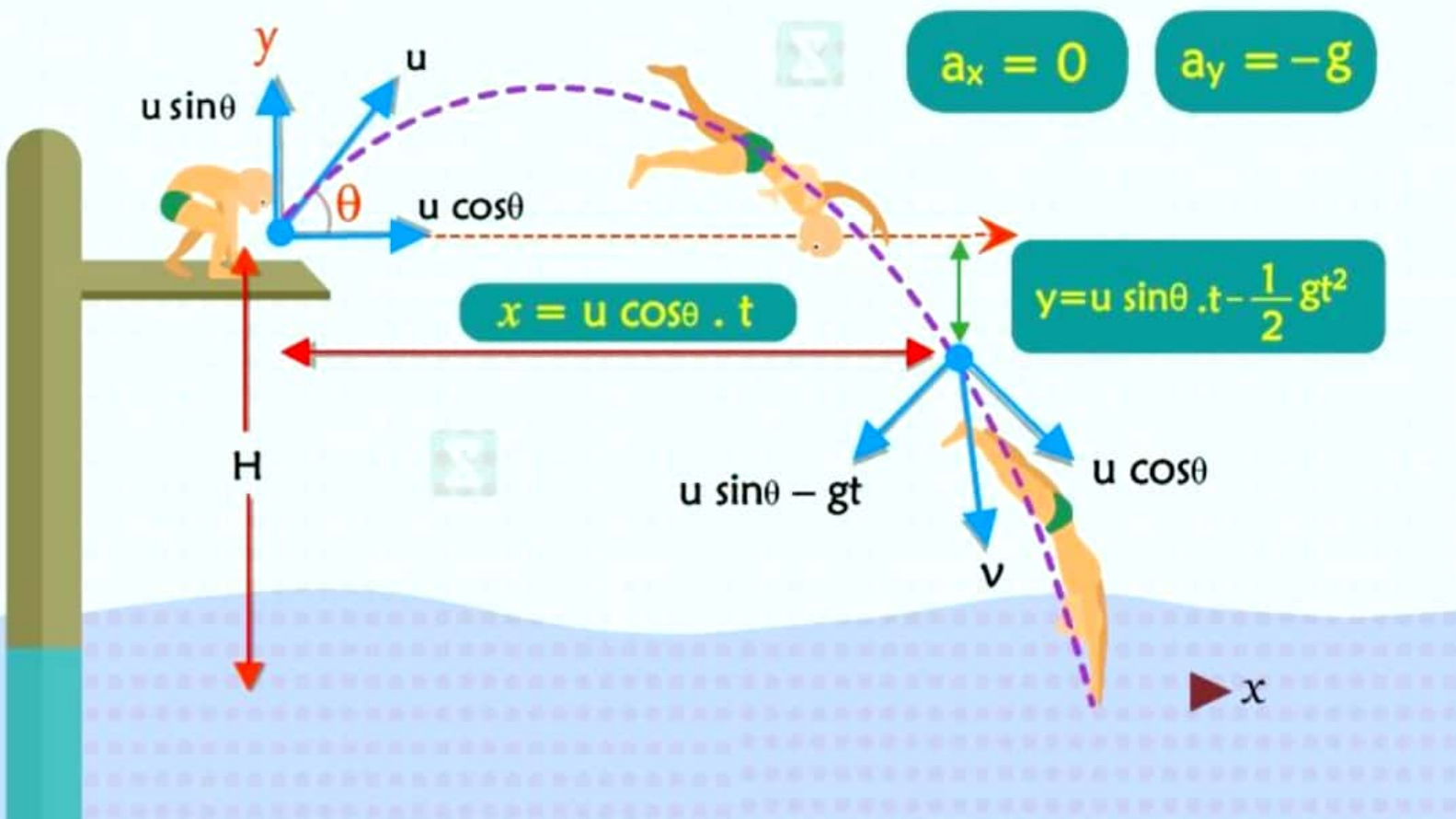




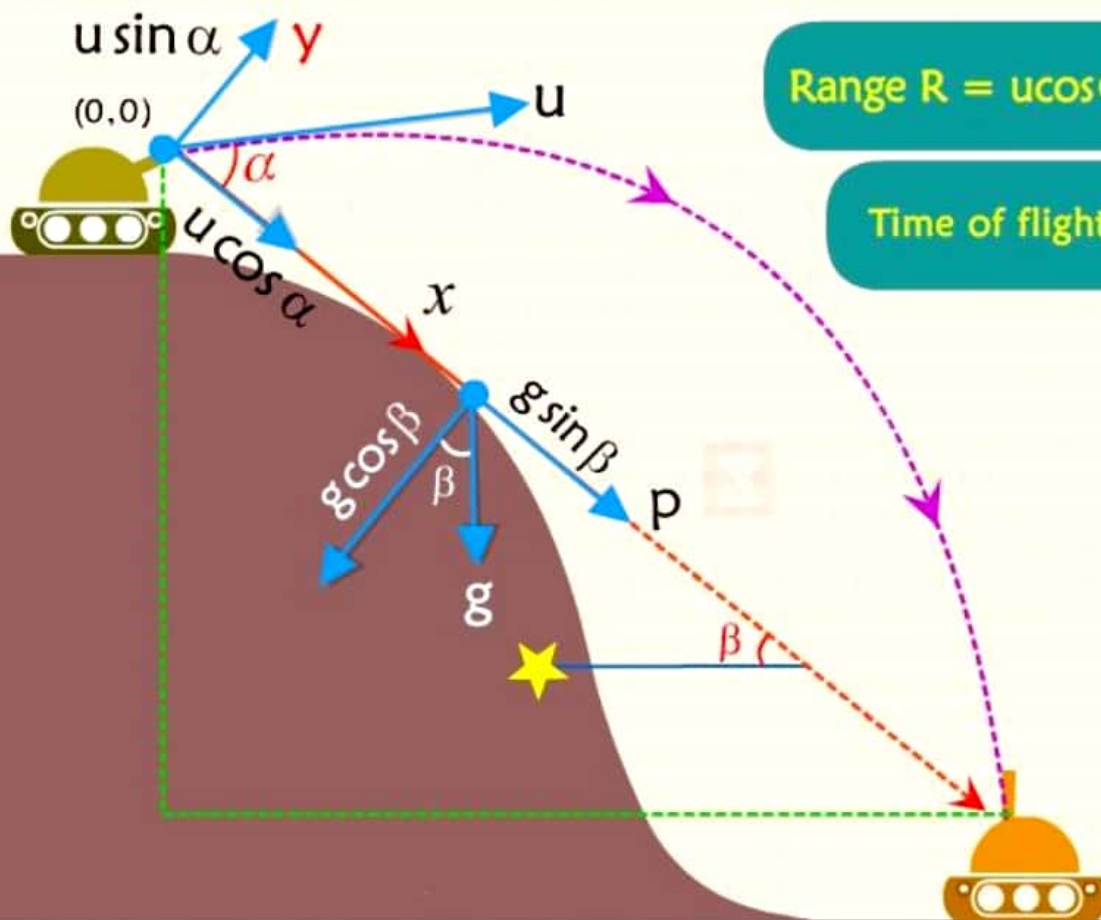
## 2 PROJECTILE FIRED PARALLEL TO HORIZONTAL



## 3 PROJECTILE AT AN ANGLE $\theta$ FROM HEIGHT 'H'



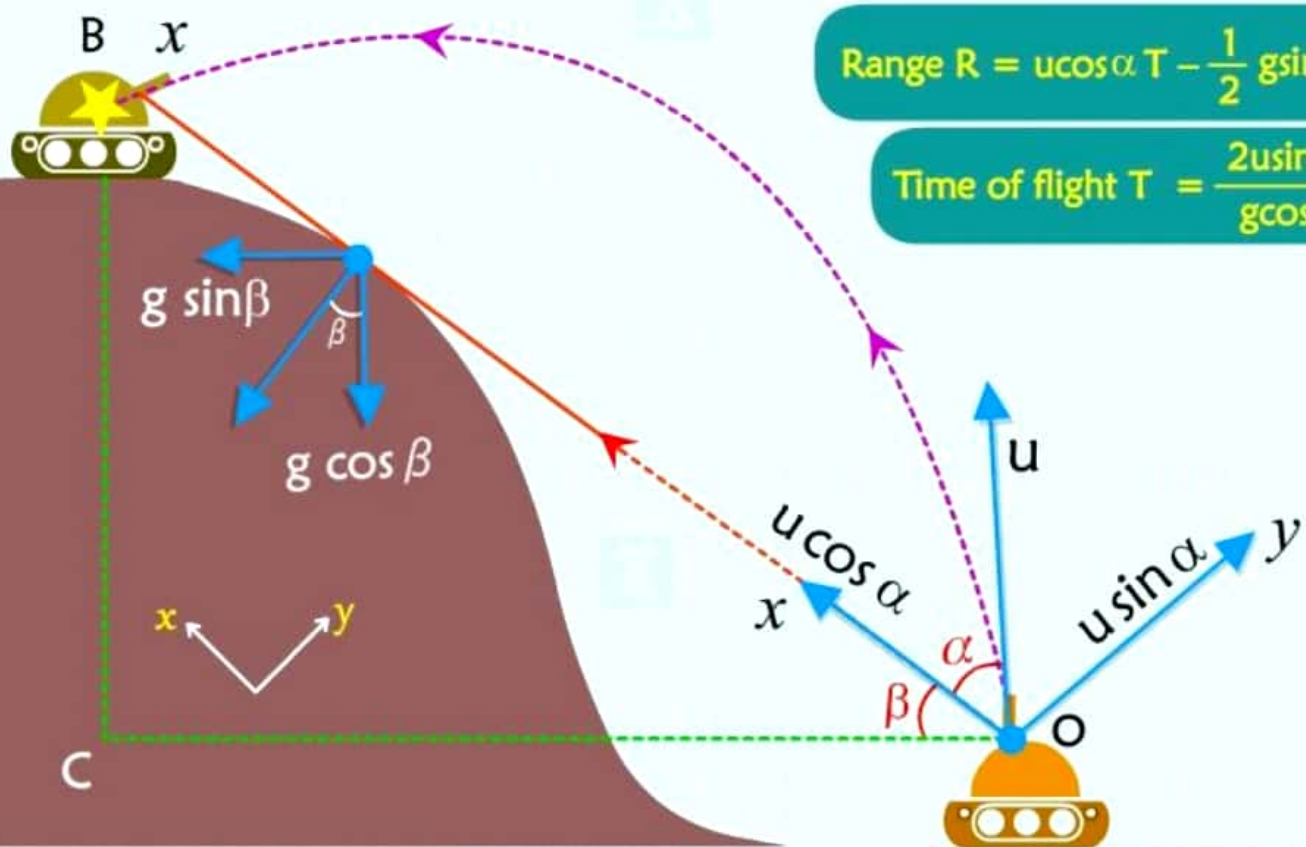
## 4 PROJECTILE MOTION DOWN THE INCLINED PLANE



$$\text{Range } R = u \cos \alpha T + \frac{1}{2} g \sin \beta T^2$$

$$\text{Time of flight } T = \frac{2u \sin \alpha}{g \cos \beta}$$

## 5 PROJECTILE MOTION UP THE INCLINED PLANE



$$\text{Range } R = u \cos \alpha T - \frac{1}{2} g \sin \beta T^2$$

$$\text{Time of flight } T = \frac{2u \sin \alpha}{g \cos \beta}$$